

U. Amsterdam

**CIFAR**

Canadian Institute for Advanced Research

# *Physics for Deep Learning & Deep Learning for Physics*

Max Welling



Uva-Qualcomm Lab



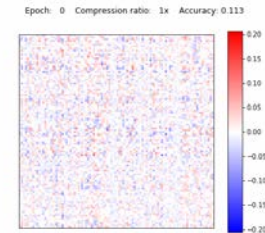
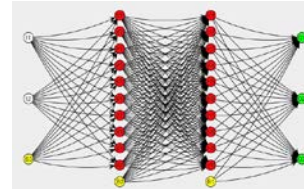
UvA - BOSCH  
**DELTA LAB**



Amsterdam  
Machine Learning Lab

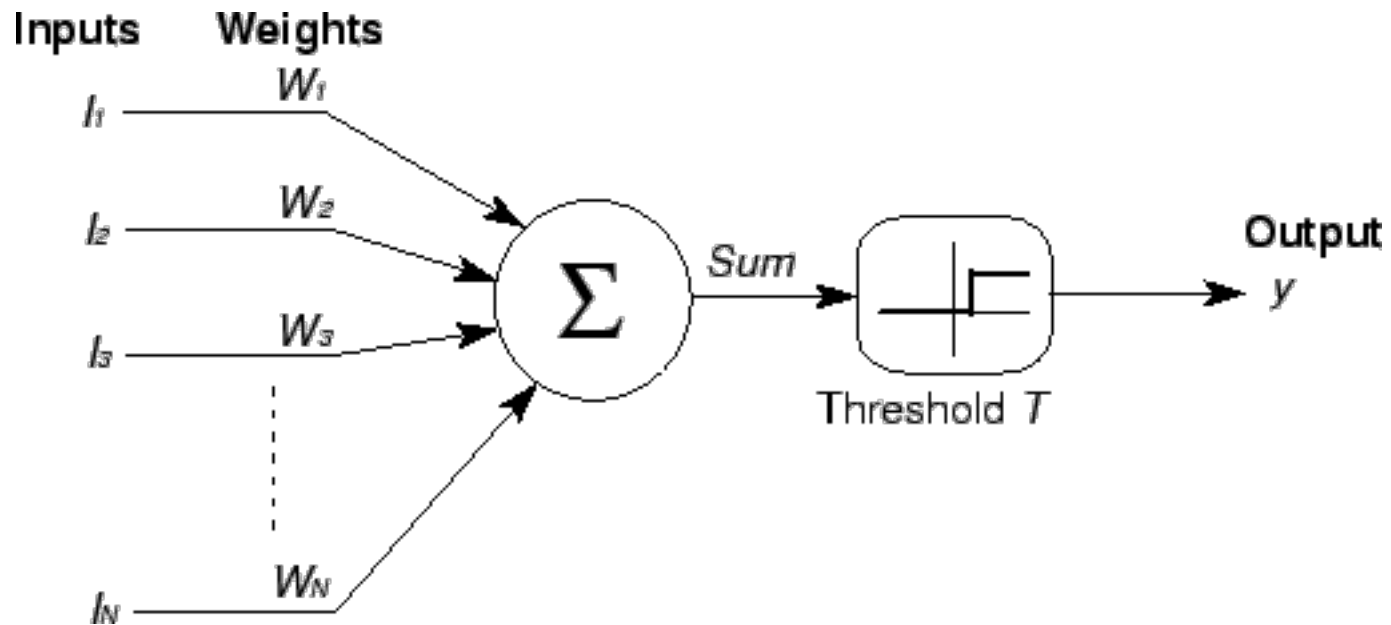
# Overview

- Part I: Deep Learning 101
- Part II: Symmetries for Deep Learning
- 
- Part III: Statistical Physics of Deep Learning
- Part IV: Deep Art



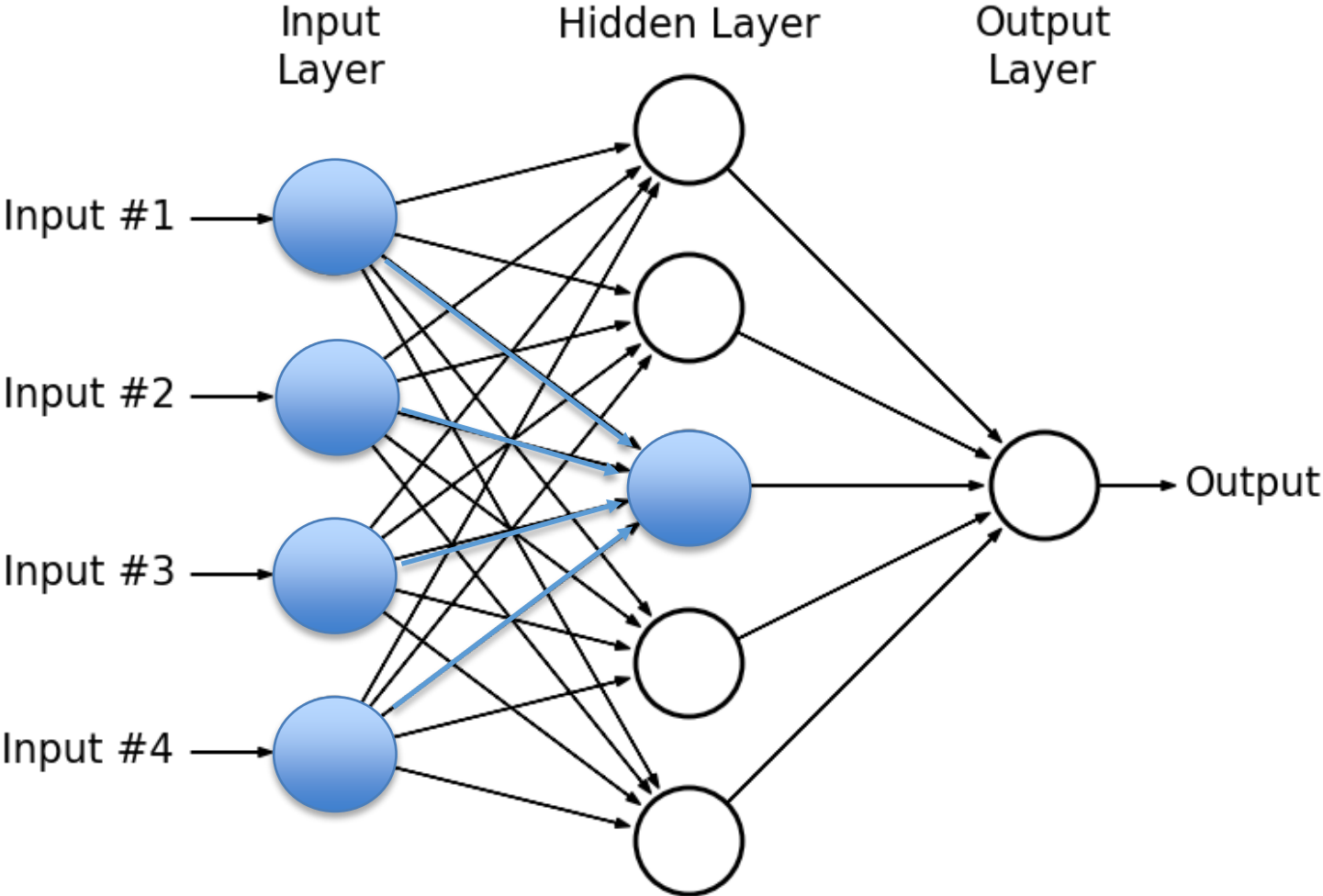
# Part I: Deep Learning 101

# 70 Years Ago



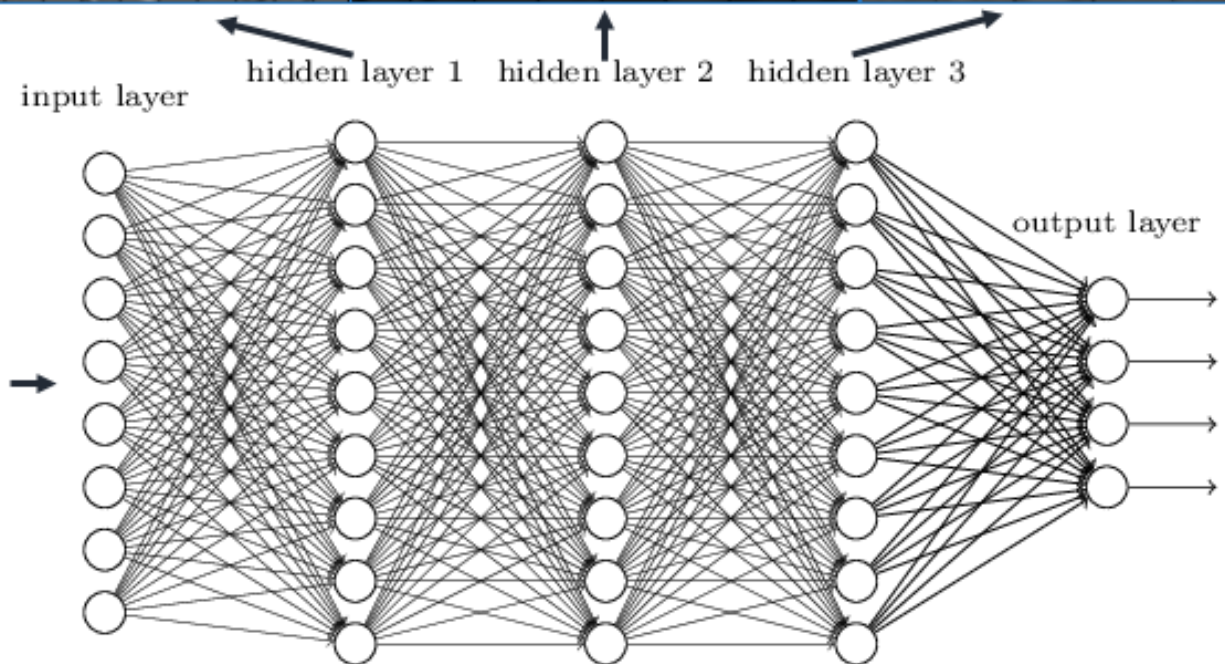
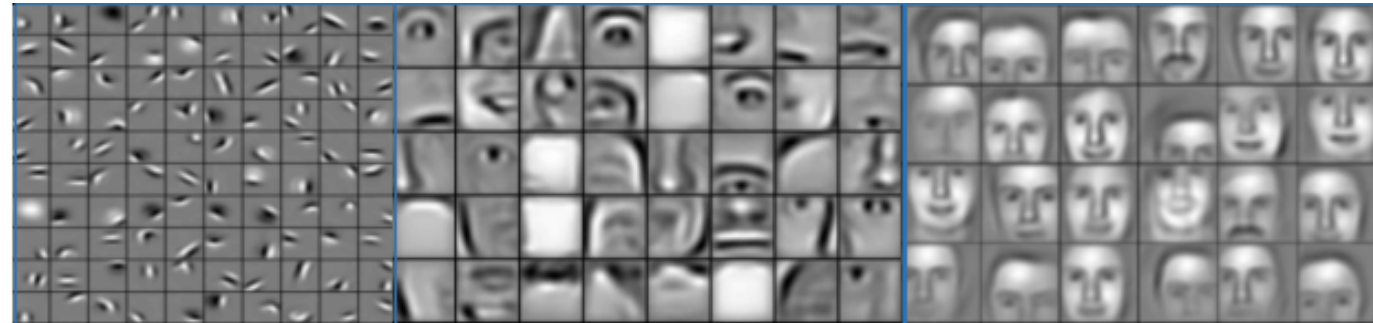
First Neural Network: McCulloch & Pitts, 1943

# 50 Years Ago



# 5 Years Ago

Deep neural networks learn hierarchical feature representations



# 1 Year Ago: Resnets

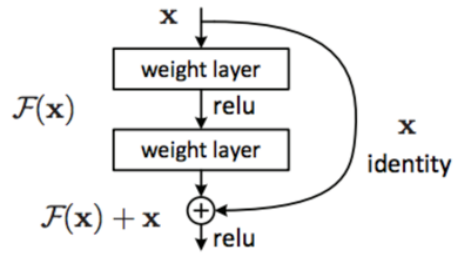
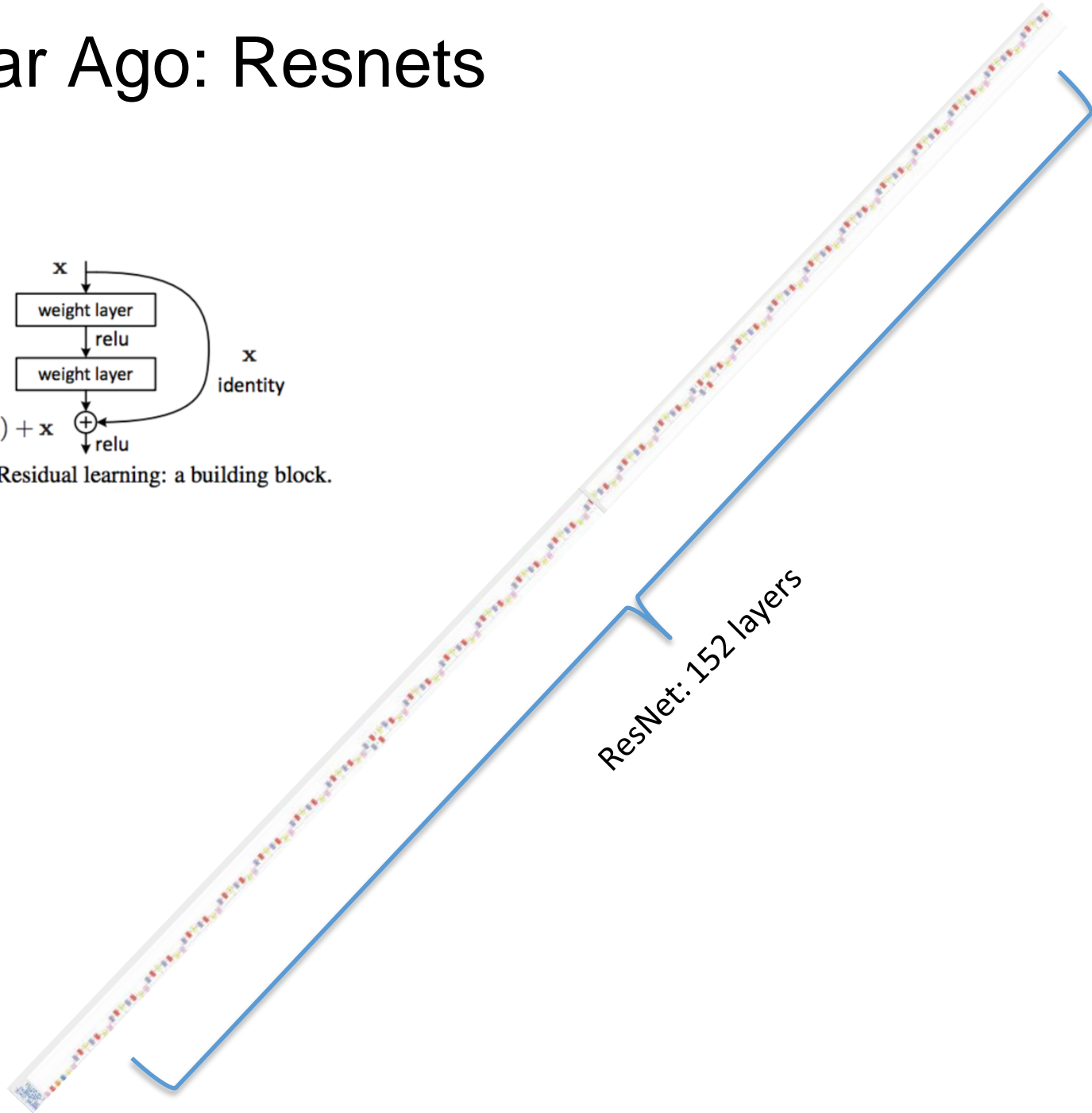


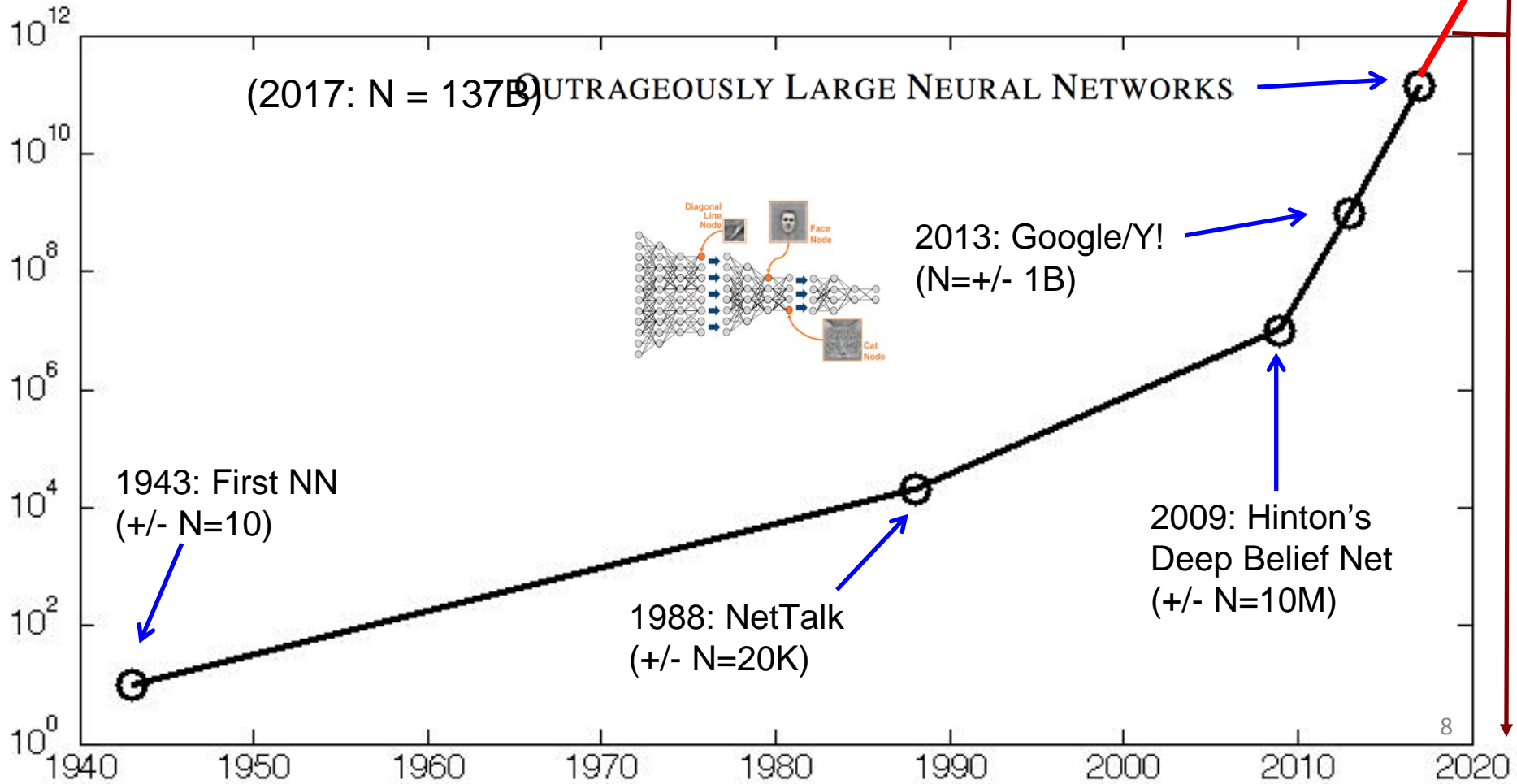
Figure 2. Residual learning: a building block.



# Explosive Growth Neural Network Capacity

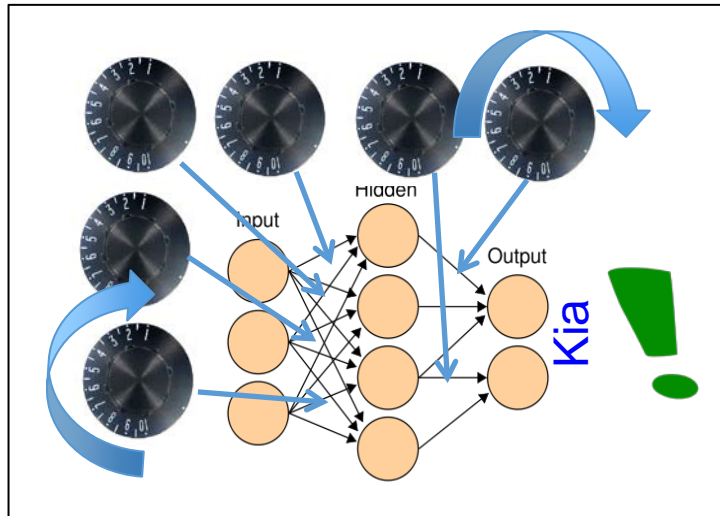
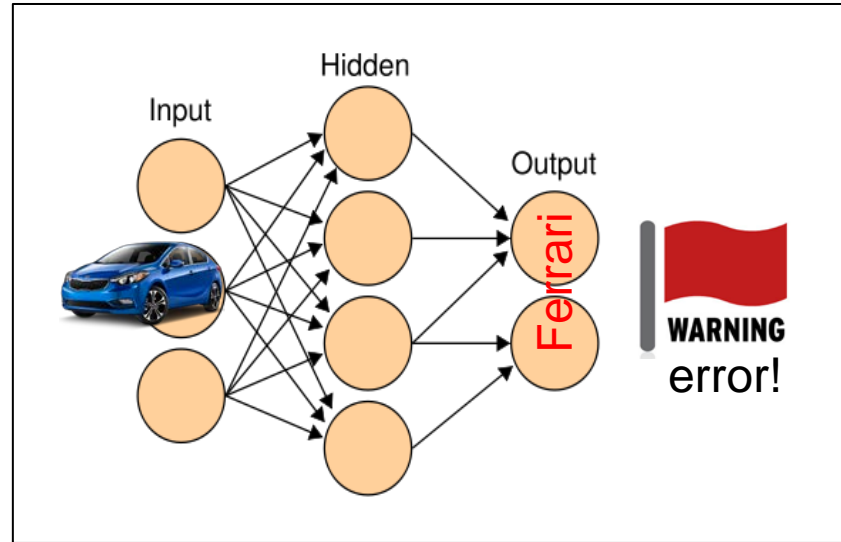
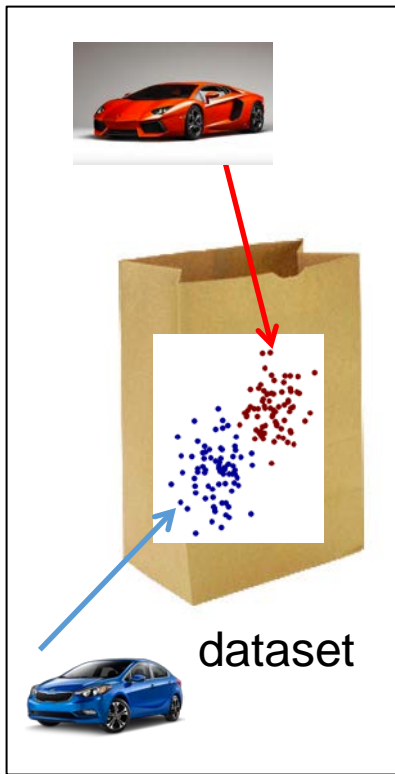


2025: capacity of human brain reached?  $N = 100T = 10^{14}$





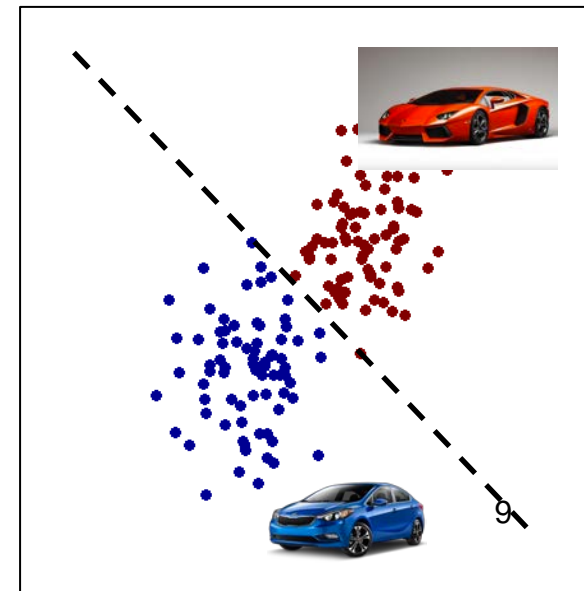
# How to Train a Computer



REPEAT



(keep turning the knobs until there are no more errors)

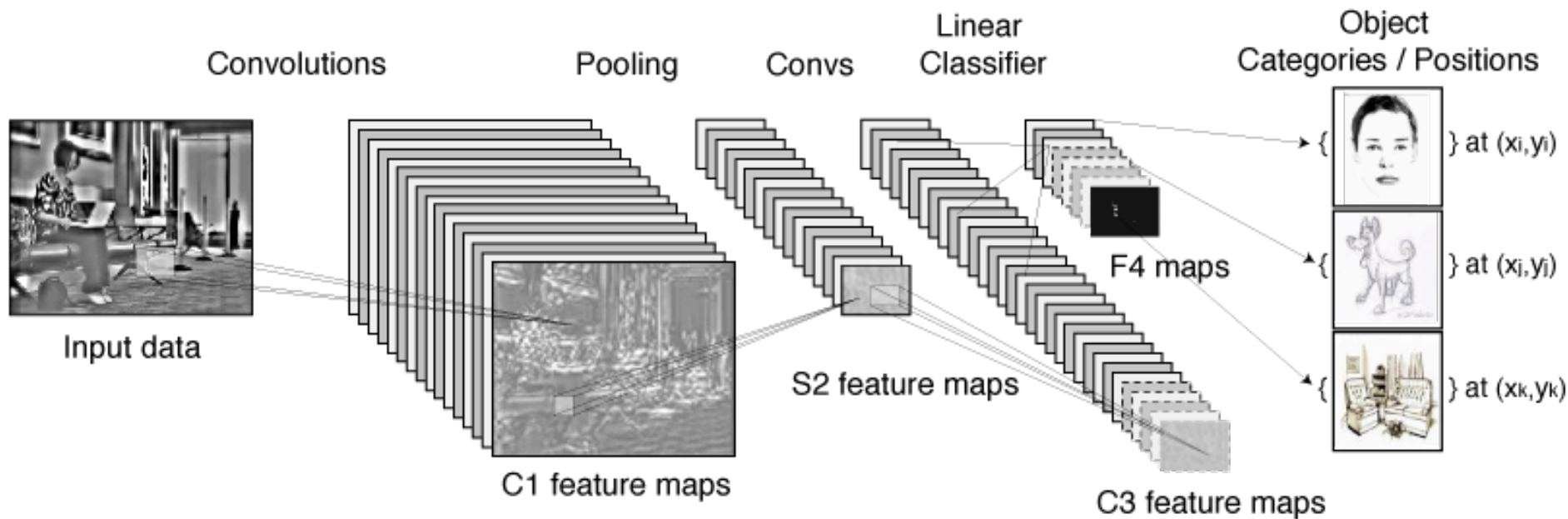


# Deep Convolutional Networks

- Input dimensions have "topology":  
(1D, speech, 2D image, 3D MRI, 2+1D video, 4D fMRI)



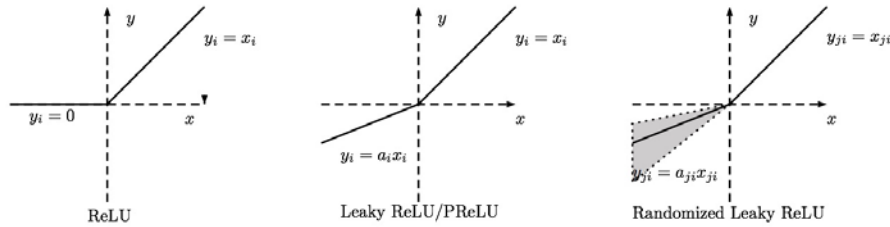
Forward: Filter, subsample, filter, nonlinearity, subsample, ....., classify



Backward: backpropagation (propagate error signal backward)

# Convolutional Network

(slide borrowed from Li Deng)



Nonlinearity



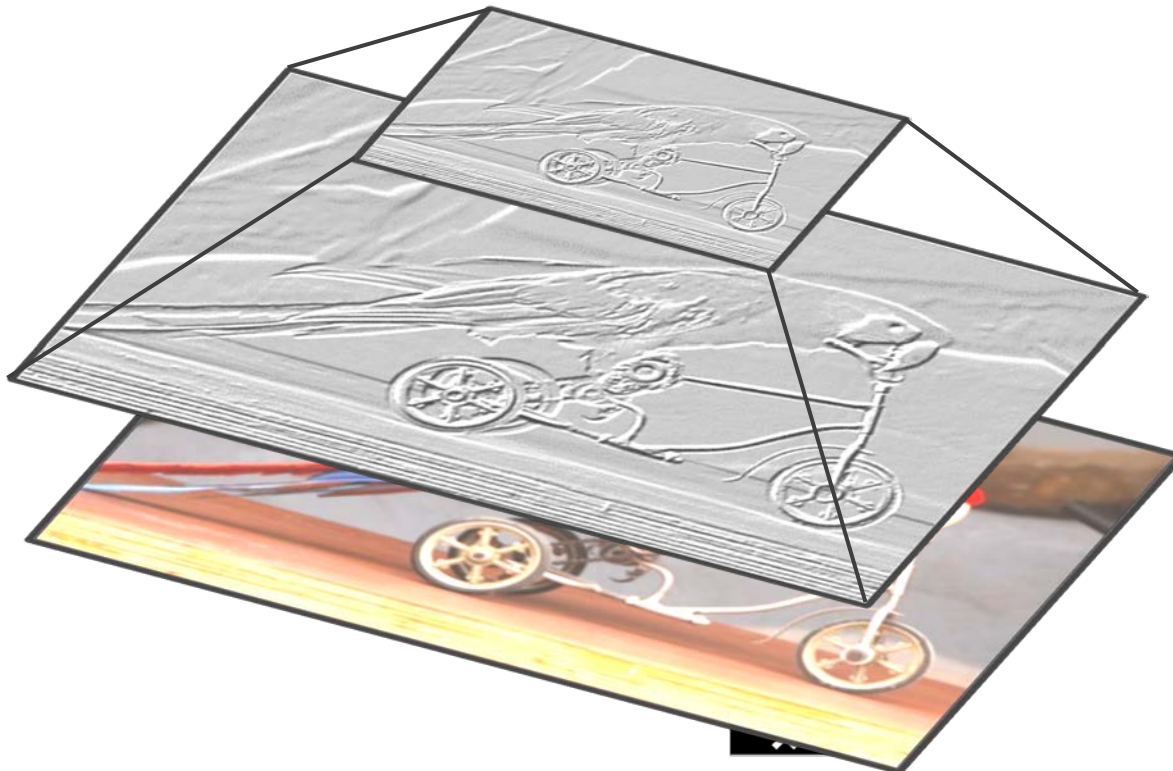
Pooling



Convolution



Image



# CNN in Action



(Andrei Karpathy's blog)

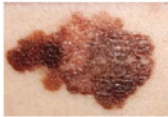


# Example: Dermatology

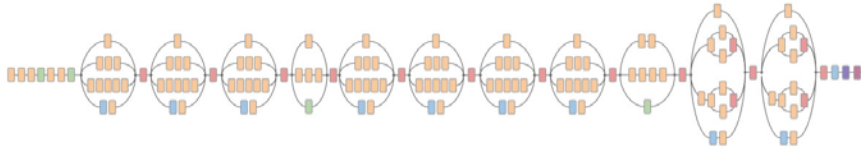
## Dermatologist-level classification of skin cancer with deep neural networks

Andre Esteva<sup>1\*</sup>, Brett Kuprel<sup>1\*</sup>, Roberto A. Novoa<sup>2,3</sup>, Justin Ko<sup>2</sup>, Susan M. Swetter<sup>2,4</sup>, Helen M. Blau<sup>5</sup> & Sebastian Thrun<sup>6</sup>

Skin lesion image



Deep convolutional neural network (Inception v3)



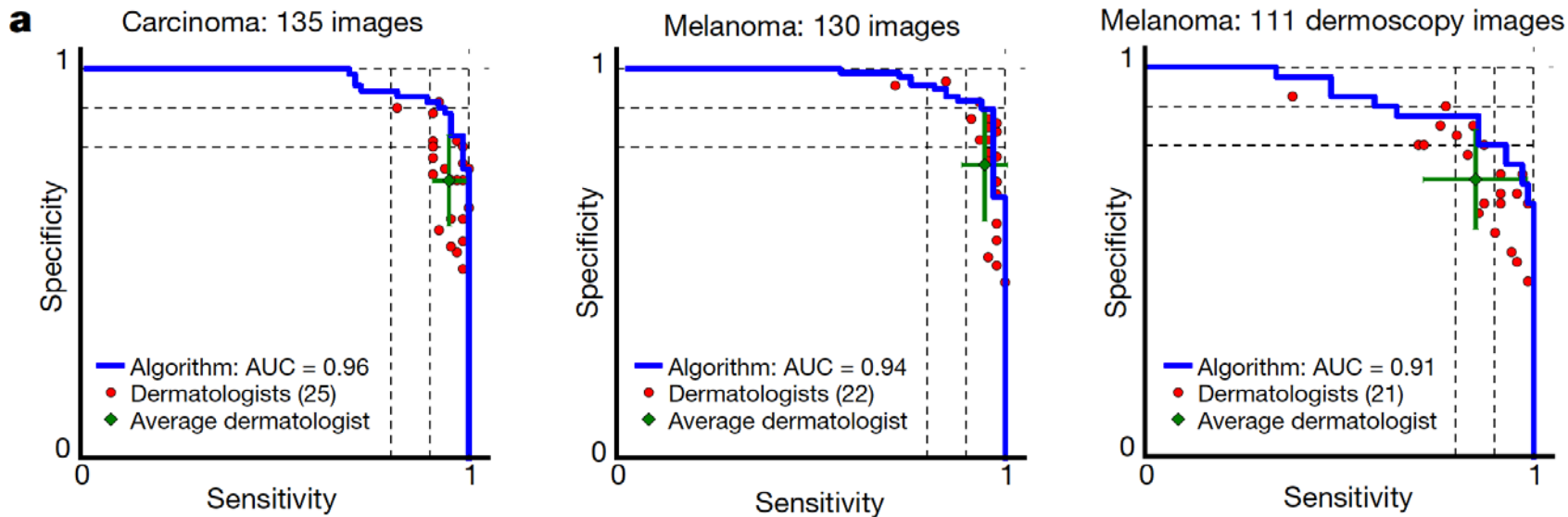
- Convolution
- AvgPool
- MaxPool
- Concat
- Dropout
- Fully connected
- Softmax

Training classes (757)

- Acral-lentiginous melanoma
- Amelanotic melanoma
- Lentigo melanoma
- ...
- Blue nevus
- Halo nevus
- Mongolian spot
- ...
- 
- 
- 

Inference classes (varies by task)

- 92% malignant melanocytic lesion
- 8% benign melanocytic lesion



# Example: Pathology

NOS

Nieuws

Sport

Uitzendingen

TELEEKST



AEX



0 km

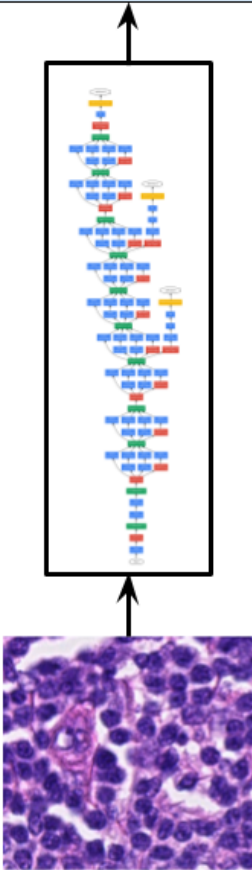
## Computer kan kanker beter herkennen dan patholoog

© VRIJDAG, 17:07 BINNENLAND, TECH

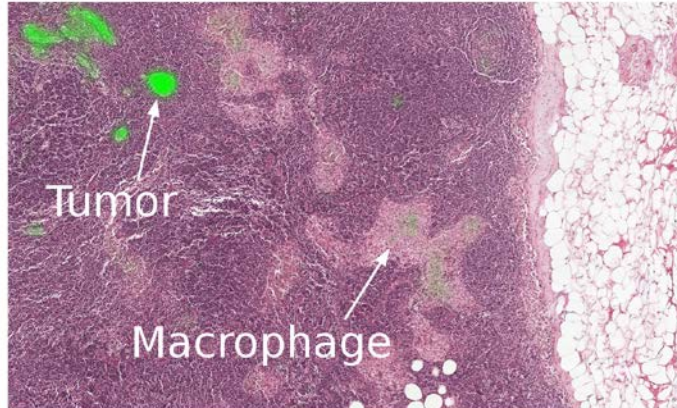


HOLLANDE HOOGTE

fully connected



40X



### Beter dan de patholoog

Datzelfde principe heeft Google nu toegepast op de data van het Radboud. Het algoritme werd geprogrammeerd om kankercellen te vinden op de foto's en vervolgens aan het werk gezet. Volgens de onderzoekers haalde het algoritme een score van 89 procent, terwijl een patholoog gemiddeld 73 procent haalt op dezelfde foto's.



# Example: Retinopathy

JAMA | **Original Investigation** | INNOVATIONS IN HEALTH CARE DELIVERY

## Development and Validation of a Deep Learning Algorithm for Detection of Diabetic Retinopathy in Retinal Fundus Photographs

Varun Gulshan, PhD; Lily Peng, MD, PhD; Marc Coram, PhD; Martin C. Stumpe, PhD; Derek Wu, BS; Arunachalam Narayanaswamy, PhD; Subhashini Venugopalan, MS; Kasumi Widner, MS; Tom Madams, MEng; Jorge Cuadros, OD, PhD; Ramasamy Kim, OD, DNB; Rajiv Raman, MS, DNB; Philip C. Nelson, BS; Jessica L. Mega, MD, MPH; Dale R. Webster, PhD

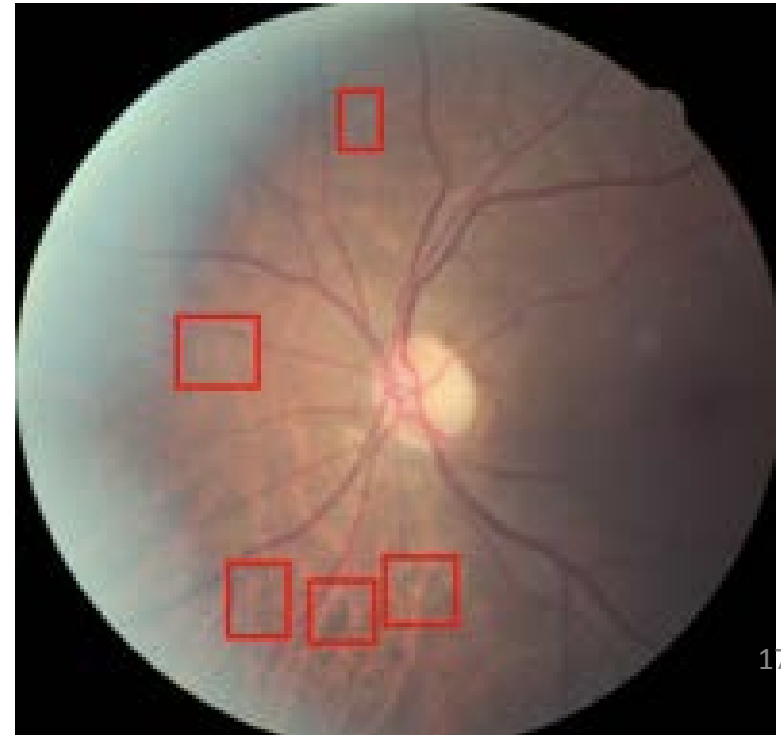
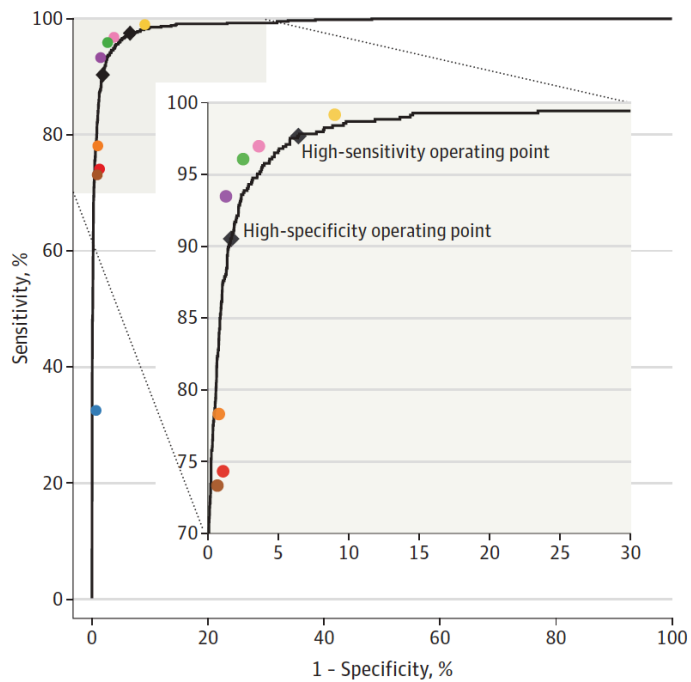
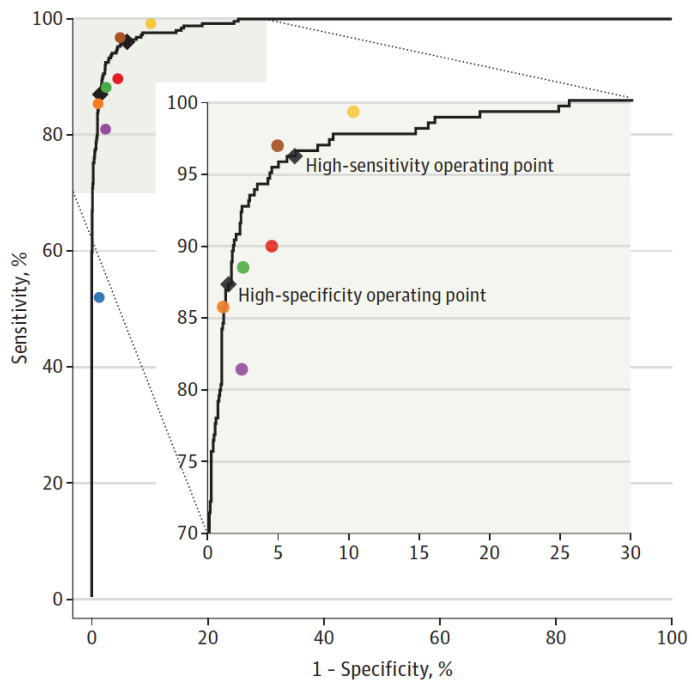


Figure 2. Validation Set Performance for Referable Diabetic Retinopathy

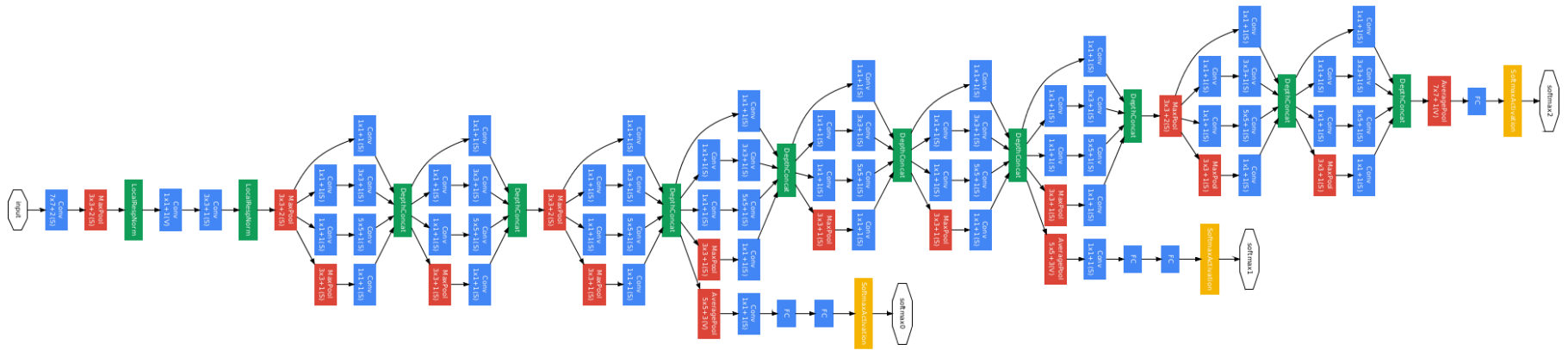
**A** EyePACS-1: AUC, 99.1%; 95% CI, 98.8%-99.3%



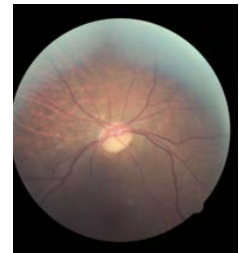
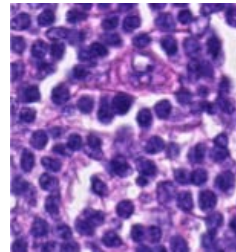
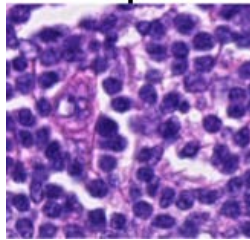
**B** Messidor-2: AUC, 99.0%; 95% CI, 98.6%-99.5%



# What do these problems have in common?



1) *It's the same CNN in all cases: Inception-v3*



1) *Object identity is translations translation, rotation, mirror invariant*

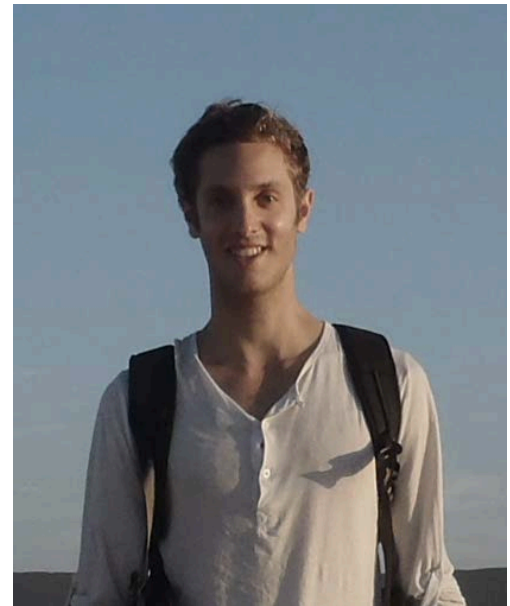
## Part II: Symmetries

# Symmetries

- How can we improve CNNs by exploiting symmetries better ?



(Escher)



Taco Cohen

# Equivariance

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi GT_{\mu\nu}$$

# Symmetry in Deep Learning

What makes CNNs so effective?

- ❖ Weight sharing: exploits translation symmetry
- ❖ Depth: exploits equivariance

Network design principle:  
*Equivariance to symmetry transformations*



(Picasso effect:  
why we do not want to  
use invariant features)

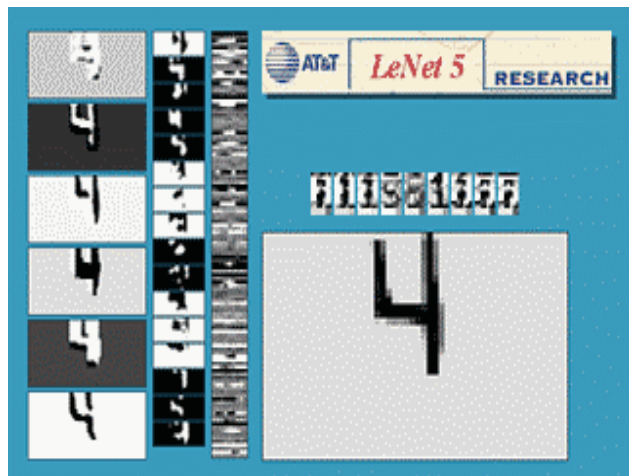
# Equivariance

$$\text{conv2d}\left(\begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array}, \begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \square \\ \hline \end{array}\right) = \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \square & \square \\ \hline \end{array}$$

$$\text{conv2d}\left(\begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array}, \begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \square \\ \hline \end{array}\right) = \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \square & \square \\ \hline \end{array}$$

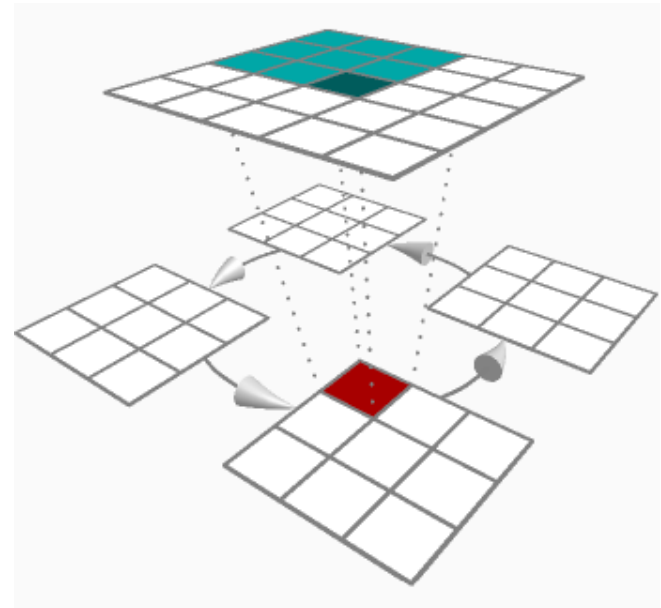
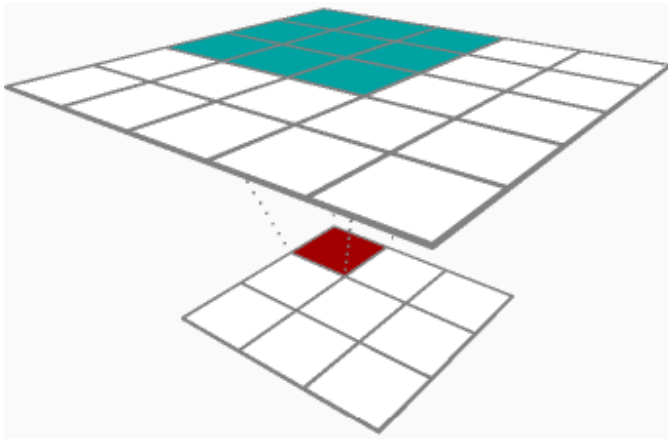


# Equivariance



Source: <http://yann.lecun.com/exdb/lenet/index.html>

# Conv vs G-Conv



T.S. Cohen & M. Welling, *Group Equivariant Convolutional Networks*. ICML 2016

J. Peters & T. Cohen, Data-Efficient Deep Learning with G-CNNs, Scyfer Blog, 2016

Sander Dieleman, Jeffrey de Fauw, Koray Kavukcuoglu, Exploiting Cyclic Symmetry in Convolutional Neural Networks, ICML2016

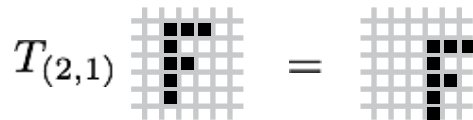
# Conv vs G-Conv

## Planar Convolution

“translate filter and compute inner product”

Translation

$$T_s f(x) = f(x - s)$$


$$T_{(2,1)}$$

$\mathbb{Z}^2$ -Convolution

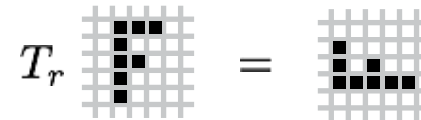
$$[f \star \psi](s) = \sum_{x \in \mathbb{Z}^2} \sum_{k=1}^K f_k(x) [T_s \psi]_k(x)$$

## Group Convolution

“transform filter and compute inner product”

Transformation

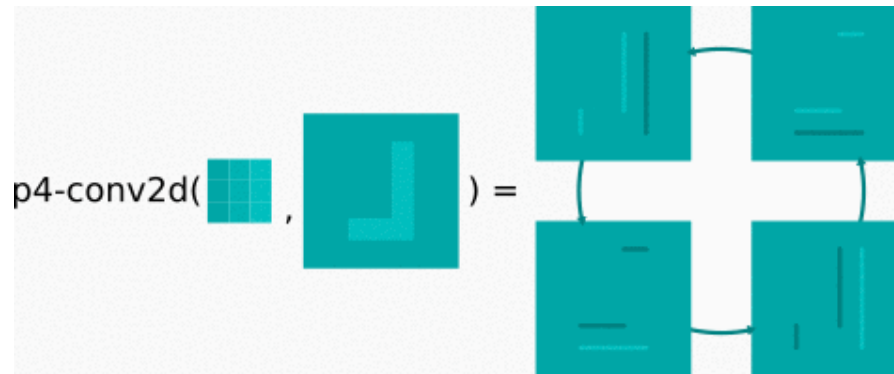
$$T_r f(x) = f(r^{-1}x)$$


$$T_r$$

G-Convolution

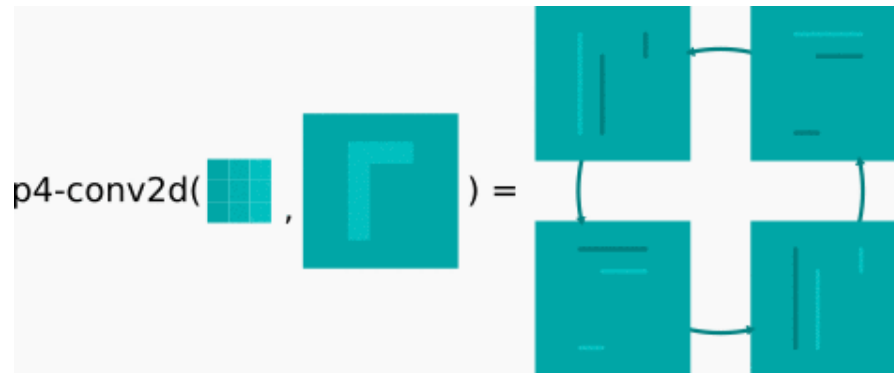
$$[f \star \psi](g) = \sum_{x \in \mathbb{Z}^2} \sum_{k=1}^K f_k(x) [T_g \psi]_k(x)$$

# Equivariance of G-Convs

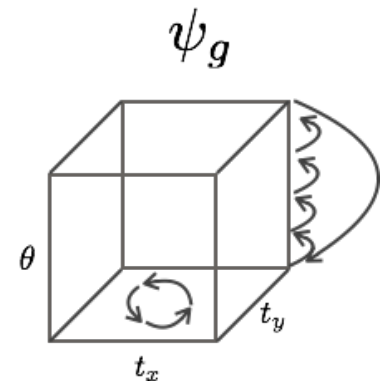


$$[T_g f] \star \psi = T_g [f \star \psi]$$

# Equivariance of G-Convs

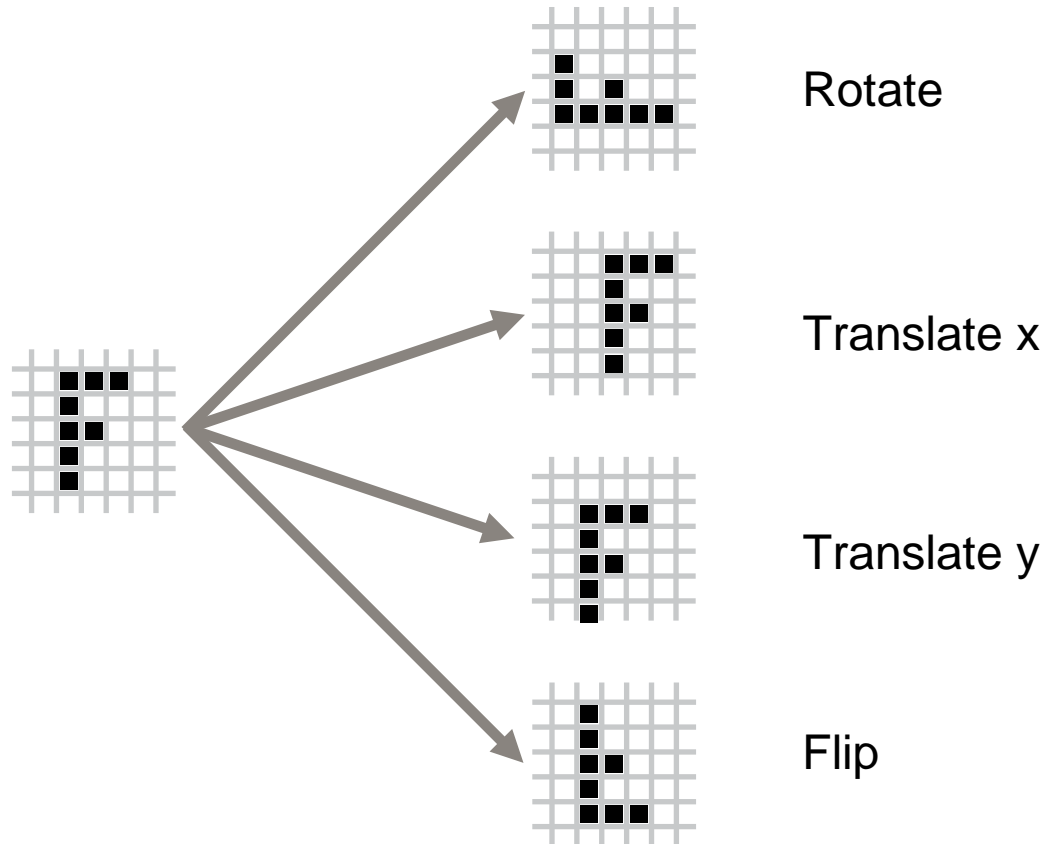


$$[T_g f] \star \psi = T_g [f \star \psi]$$

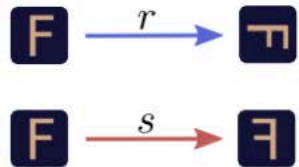
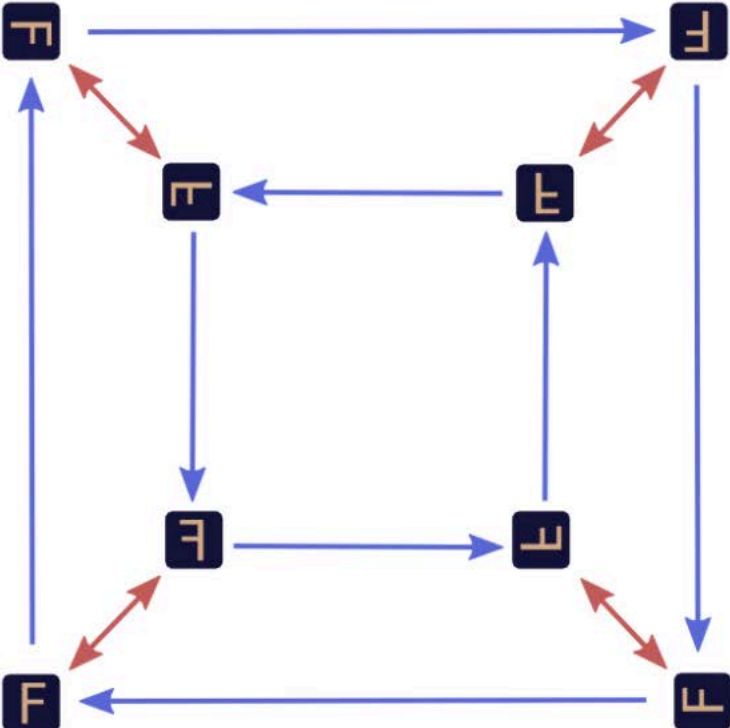




# The Groups p4 & p4m



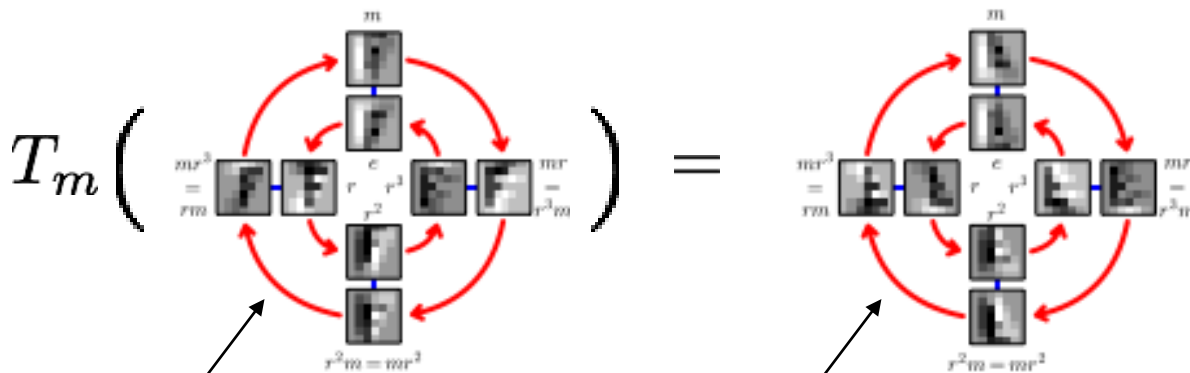
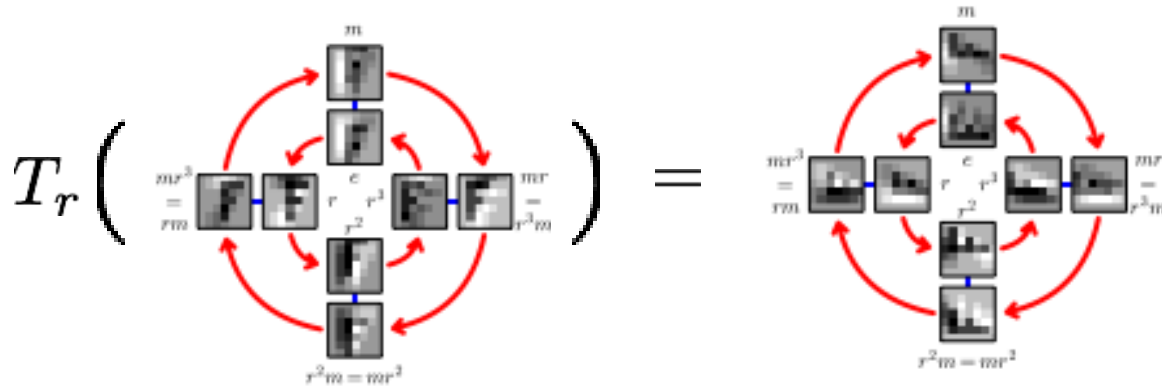
# Cayley Diagrams



(from Olah's blog)

# Equivariance of G-Convs

$$[T_g f] \star \psi = T_g[f \star \psi]$$



(result of gconv on "F")

(The filter maps transform and permute)



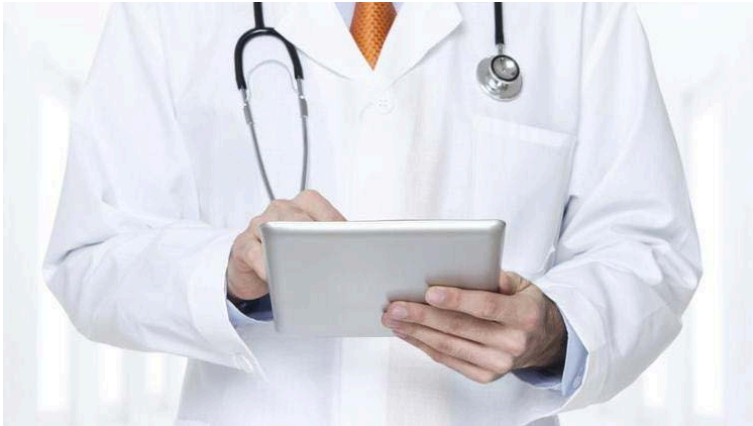
# Some Results

Network	Group	CIFAR10	CIFAR10+
All-CNN	$Z_2$	9.44	8.86
	$p4$	8.84	7.67
	$p4m$	7.59	7.04
ResNet44	$Z_2$	9.45	5.61
	$p4m$	6.46	4.94

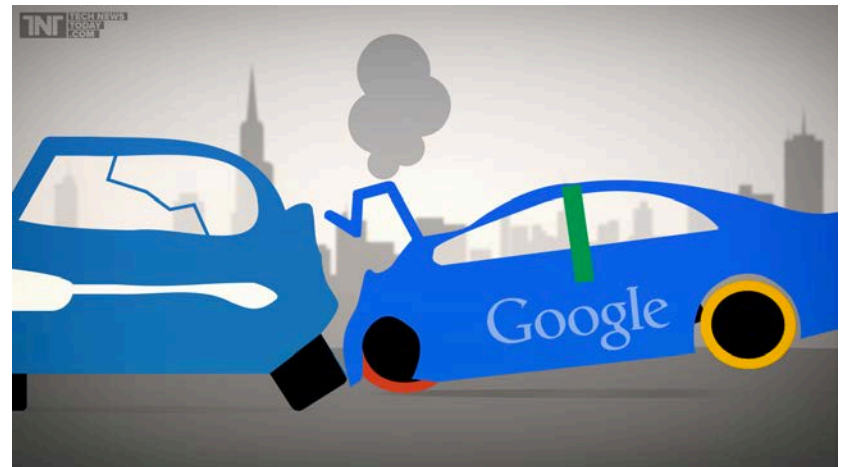
# PART III: Bayesian Deep Learning

# Reasons for Bayesian Deep Learning

- Automatic model selection / pruning
- Automatic regularization
- Realistic prediction uncertainty (important for decision making)

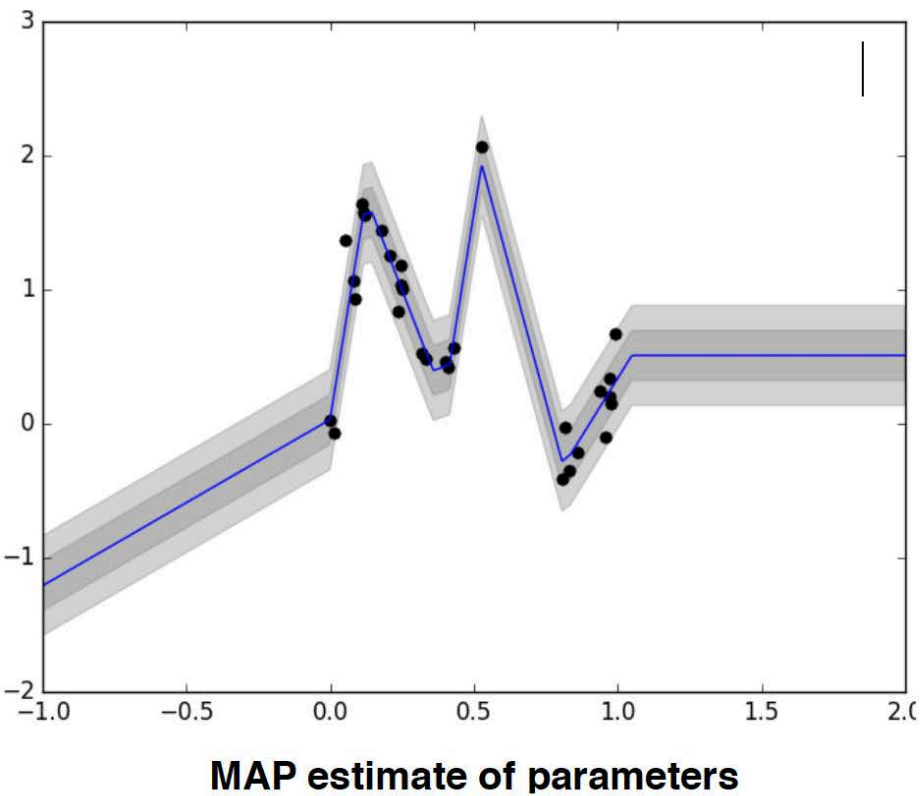


Computer Aided Diagnosis

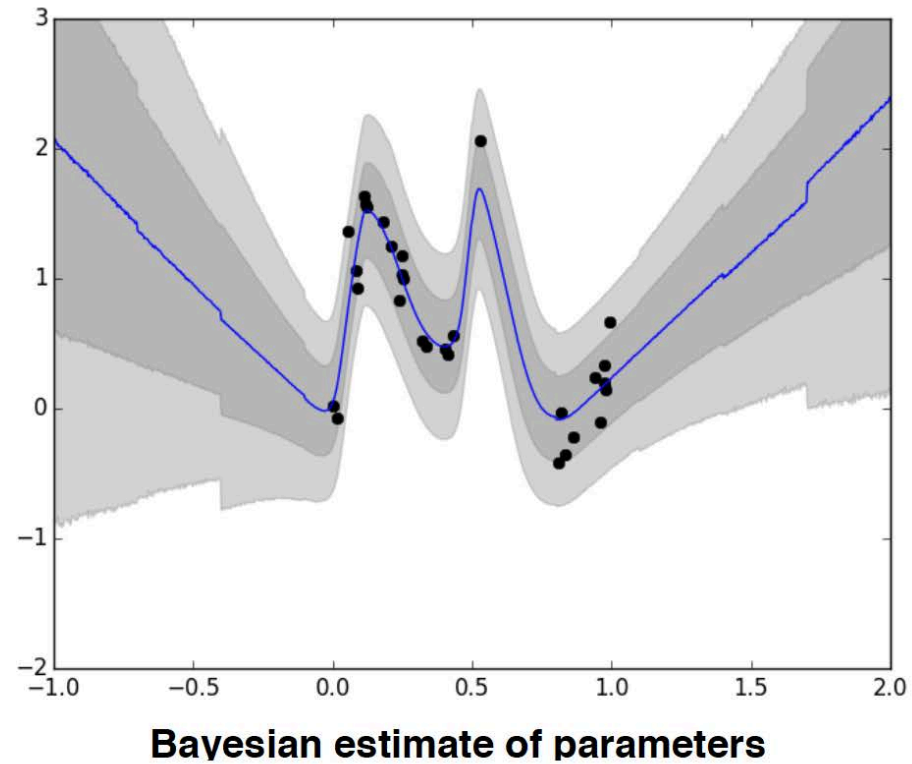


Autonomous Driving

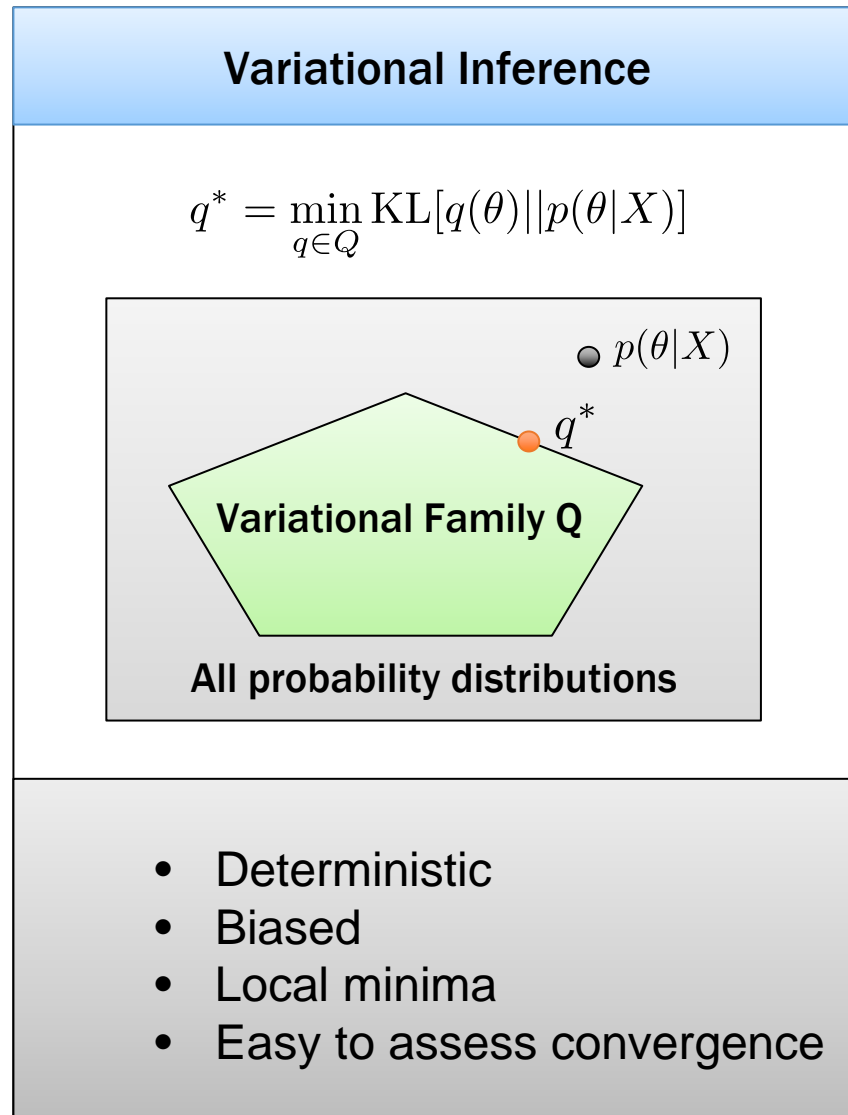
# Example



Increased uncertainty away from data

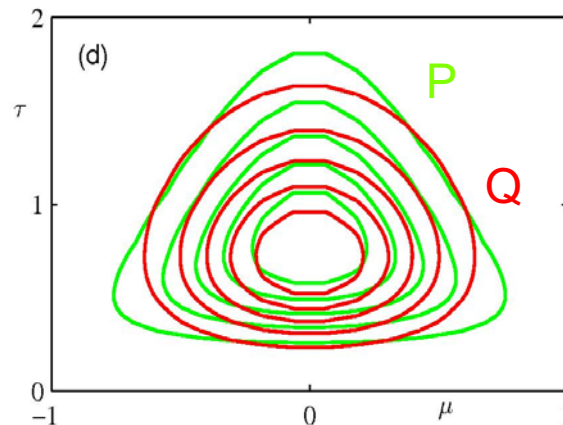


# Bayesian Variational Posterior Inference



# Deep Learning as Statistical Physics

$$\begin{aligned} -F(Q(\Theta)|X) &= \int d\Theta \overset{\text{Energy } E}{Q(\Theta)} [\log(P(X|\Theta)P(\Theta)) - \log Q(\Theta)] \\ &= \log P(X) - \overset{\text{Entropy } H}{KL} [Q(\Theta)||P(\Theta|X)] \\ &\leq \log P(X) \end{aligned}$$



(Bishop, Pattern Recognition and Machine Learning)

# Sparsifying & Compressing CNNs



w/ Karen Ullrich and Ted Meeds

- DNNs are vastly overparameterized (e.g. distillation, Bucilua et al 2006).
- Interpret variational bound as coding cost for data (minimum description length)

$$\mathcal{L}(q, \mathbf{w}) = -\mathbb{E}_q \left[ \log \left( \frac{p(\mathcal{D}|\mathbf{w})p(\mathbf{w})}{q} \right) \right] = \underbrace{\mathbb{E}_q [-\log p(\mathcal{D}|\mathbf{w})]}_{L^E} + \underbrace{\text{KL}(q||p(\mathbf{w}))}_{L^C}$$

error loss  $\sim N$                       complexity loss  $\sim \text{const.}$

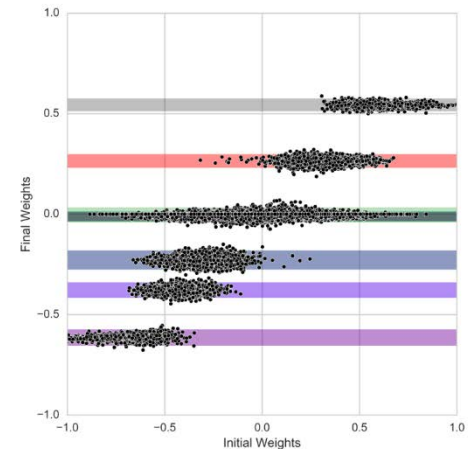
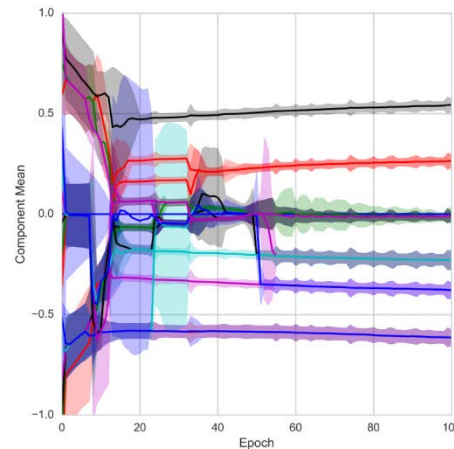
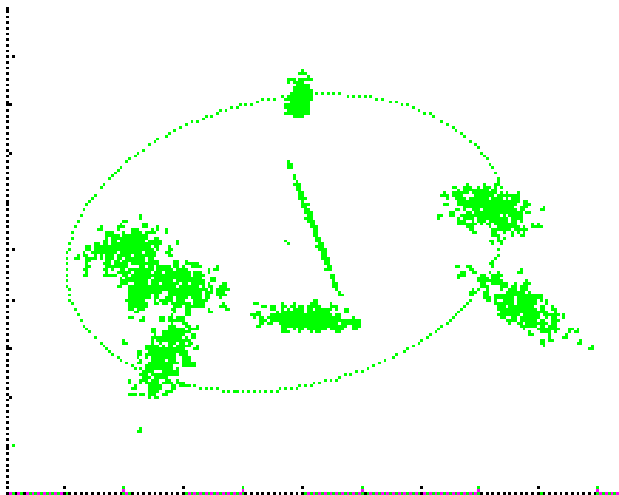
# Empirical Bayes

- Simple idea: learn a soft weight sharing prior (Nowlan & Hinton 1991, Gong et al 2014)

- Fit "Mixture of Gaussians" prior to the distribution of weights (Nowlan & Hinton 1991).

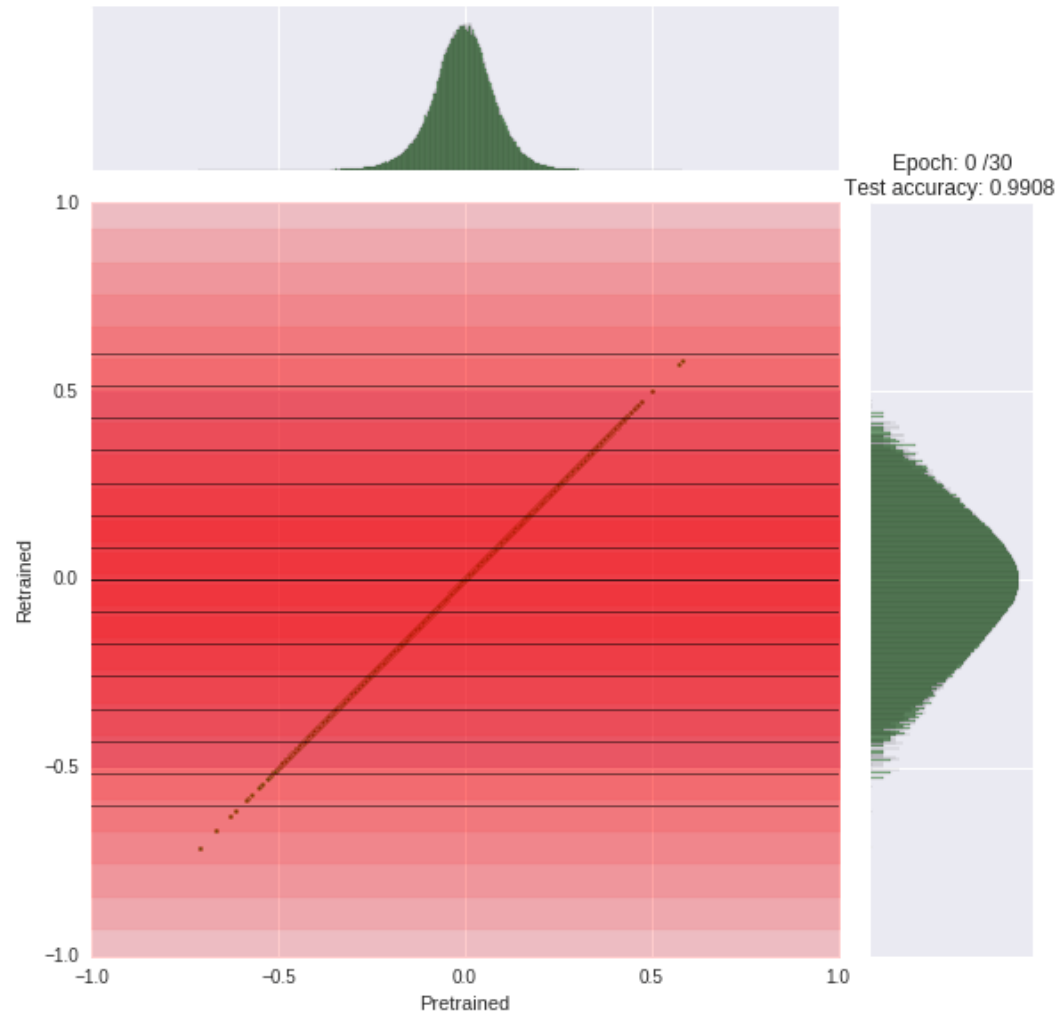
$$p(\mathbf{w}) = \prod_{i=1}^I \sum_{j=0}^J \pi_j \mathcal{N}(w_i | \mu_j, \sigma_j^2)$$

- Fixed component at  $w=0$  encouraged to be very large (large  $\pi_0$ ).
- When training likelihood and prior jointly, the weights cluster.





# Clustering and Sparsification of the Network Weights

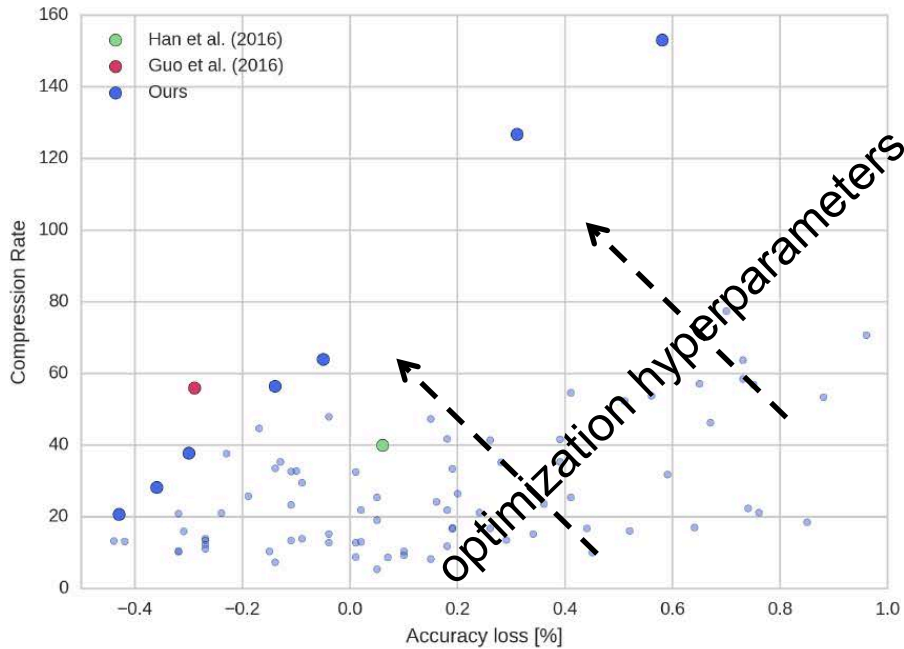


# Some Results

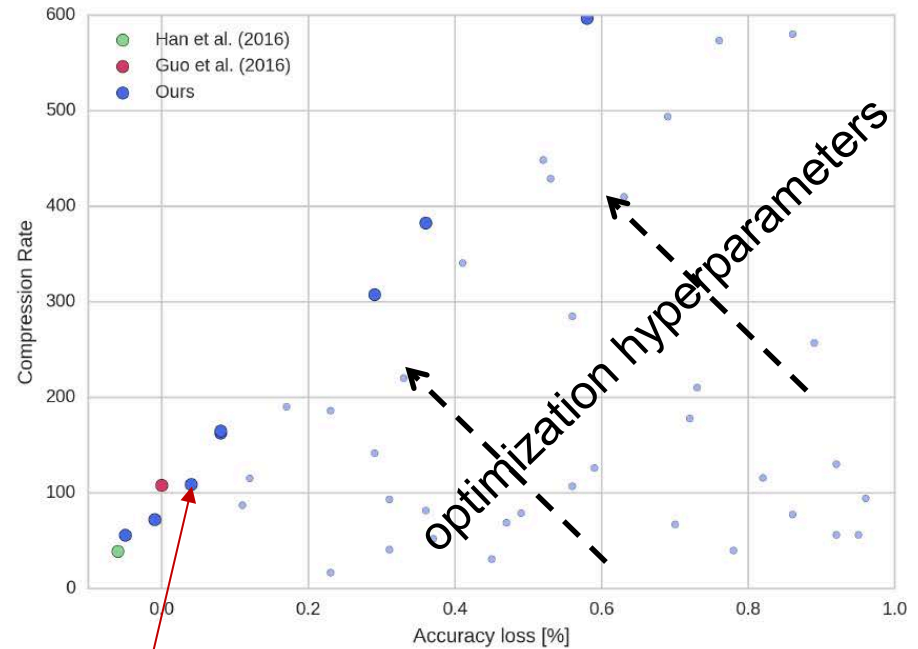
Encode cluster means

Encode for each weight to which cluster it belongs

## LeNet-300-100

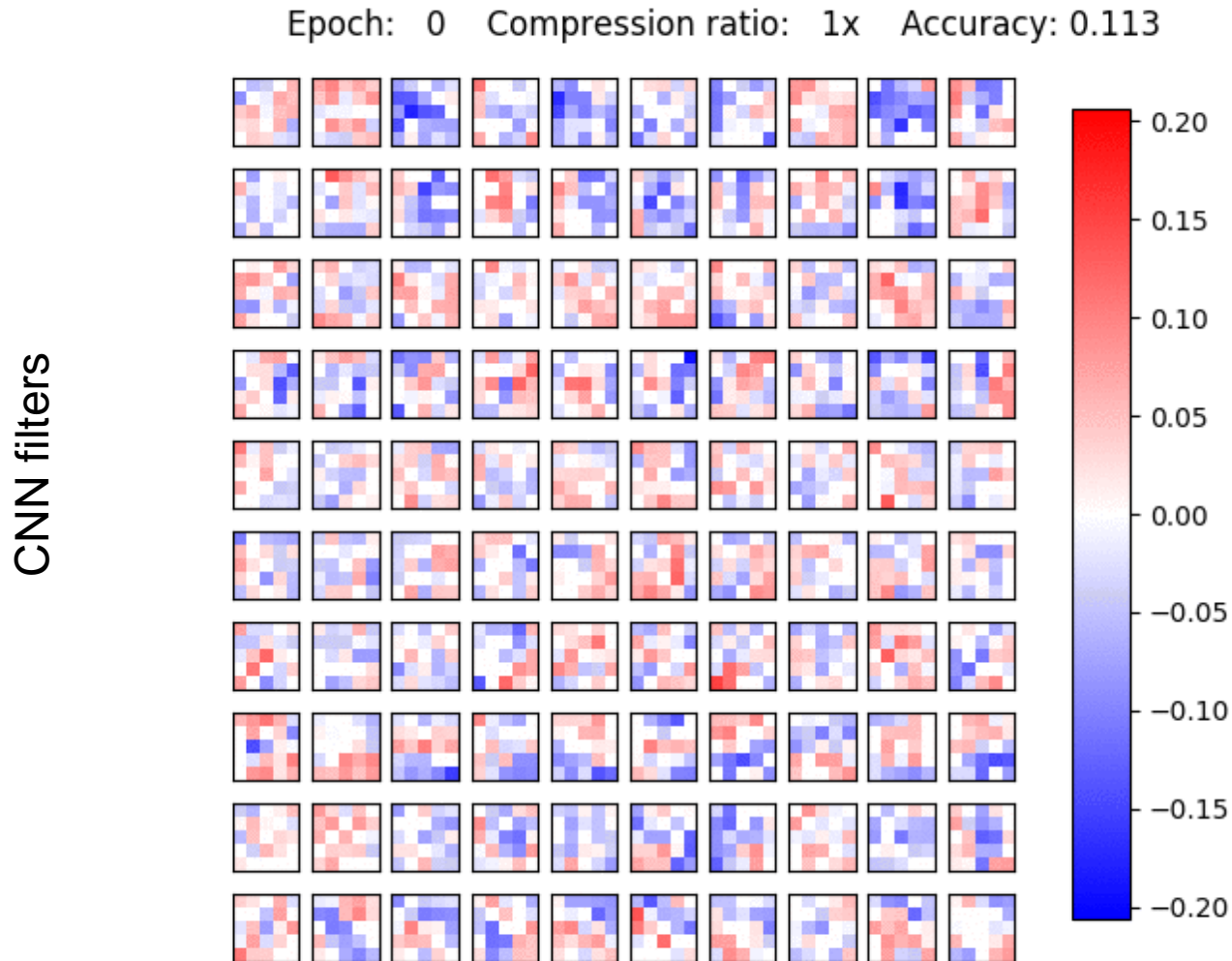


## LeNet-5-Caffe



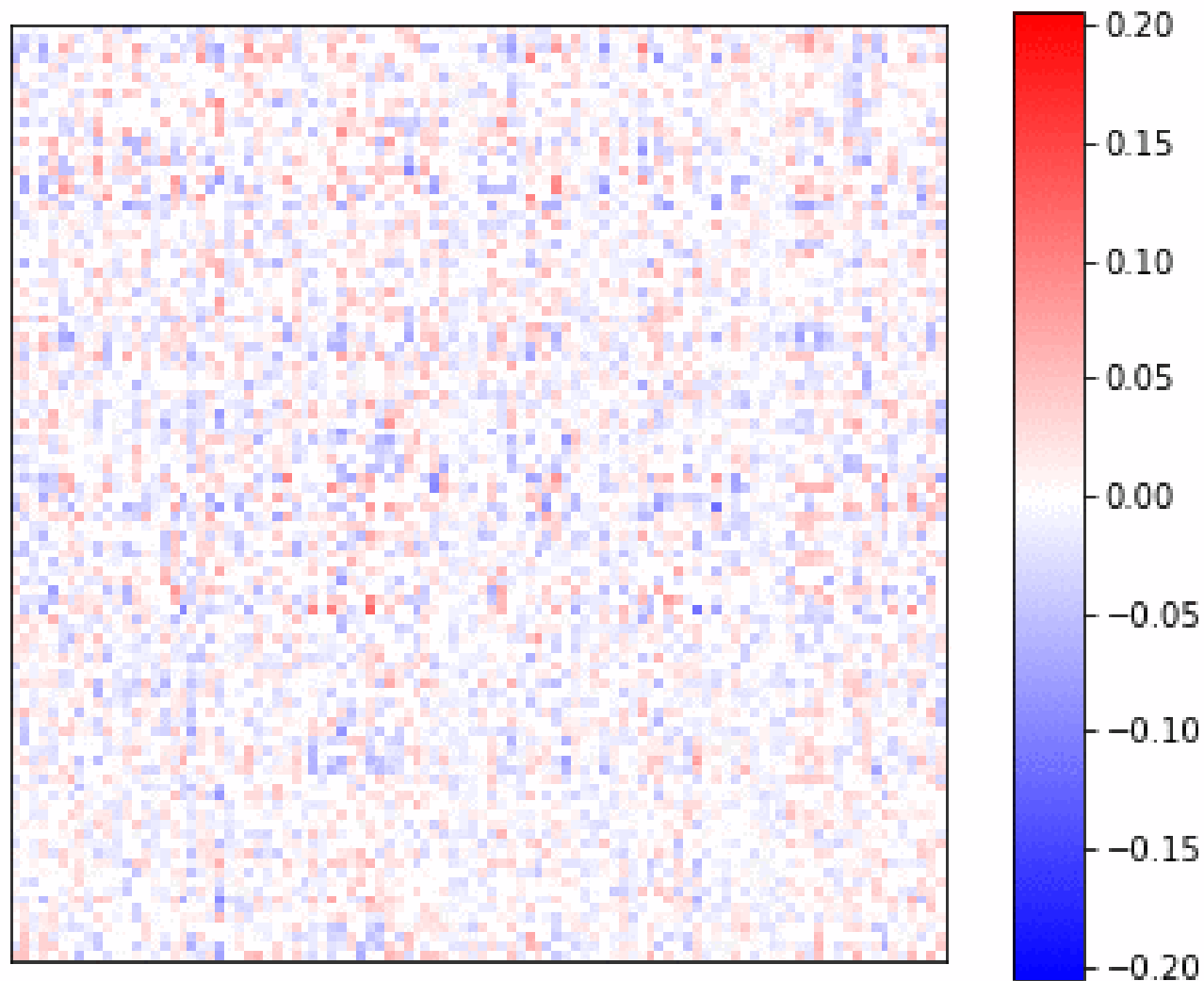
*100 fold compression with almost no loss in accuracy.*

# Variational Dropout



Epoch: 0 Compression ratio: 1x Accuracy: 0.113

Fully connected layer



Animation: Molchanov, D., Ashukha, A. and Vetrov, D.

# Preliminary Results

(Louizos, Ullrich, Molchanov, Vetrov, Welling 2017, unpublished)

Network & size	Method	Pruned architecture	Bit-precision
LeNet-300-100	Sparse VD	512-114-72	8-11-14
784-300-100	GNJ	278-98-13	8-9-14
	GHS	311-86-14	13-11-10
LeNet-5-Caffe	Sparse VD	14-19-242-131	13-10-8-12
20-50-800-500	GD	7-13-208-16	-
	GL	3-12-192-500	-
	GNJ	8-13-88-13	18-10-7-9
VGG	GHS	5-10-76-16	10-10-14-13
	GNJ	63-64-128-128-245-155-63- -26-24-20-14-12-11-11-15	10-10-10-10-8-8-8- -5-5-5-5-5-6-7-11
(2× 64)-(2× 128)- (3× 256)-(8× 512)	GHS	51-62-125-128-228-129-38- -13-9-6-5-6-6-6-20	11-12-9-14-10-8-5- -5-6-6-6-8-11-17-10

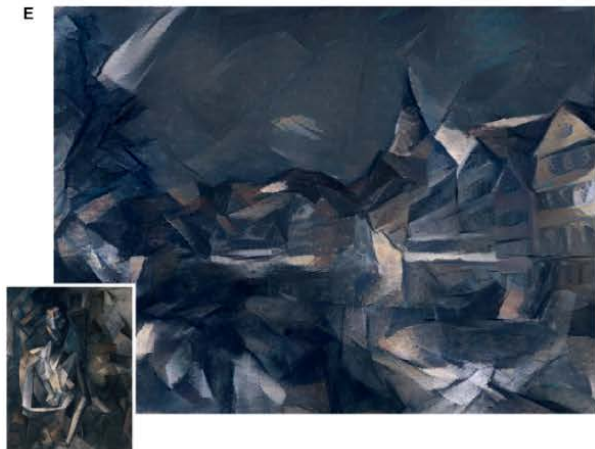
← *Additional Bayesian Bonus:*  
By monitoring posterior fluctuations of weights one can determine their fixed point precision.

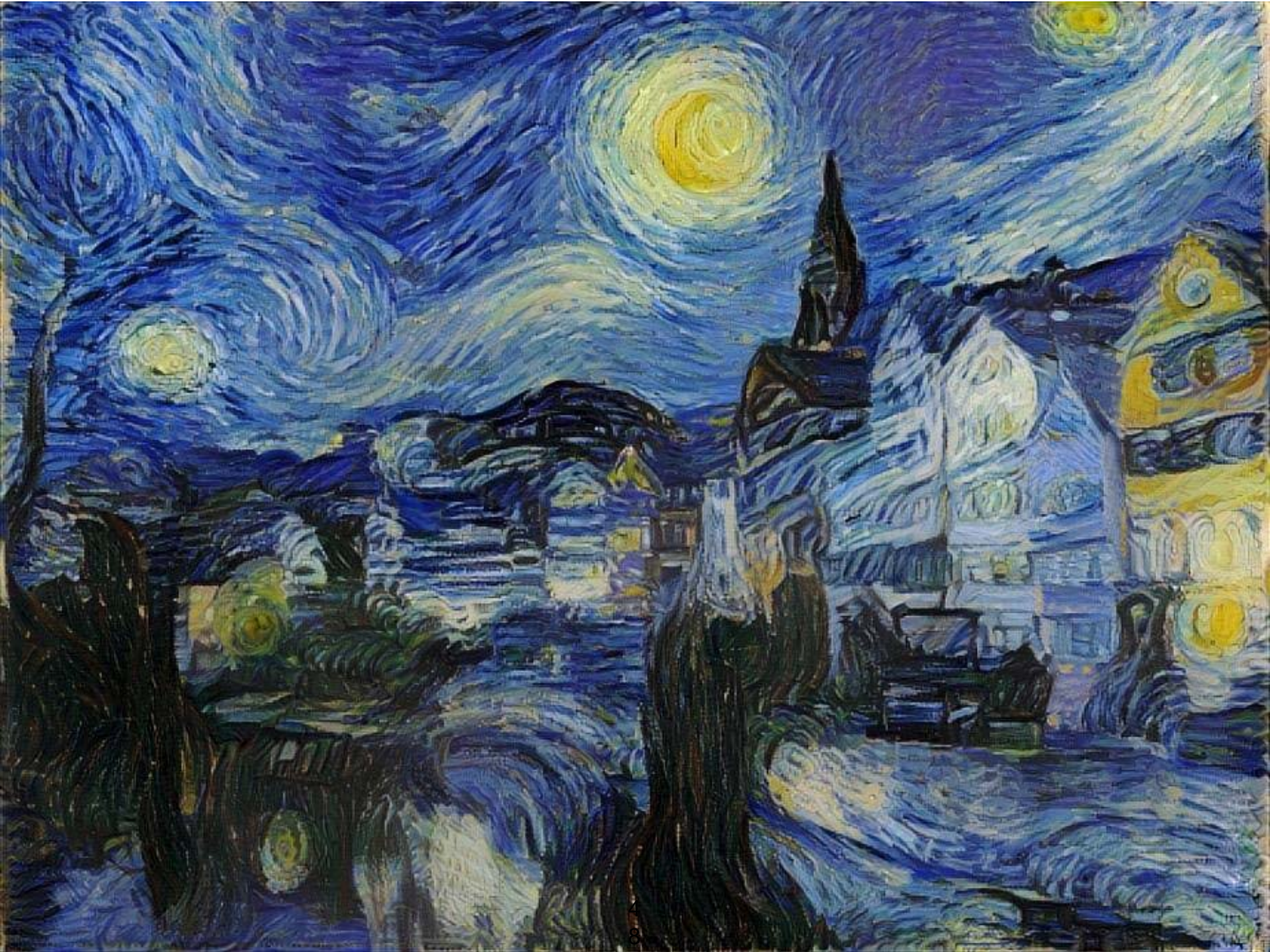
Model	Original Error %	Method	Compression Rates (Error %)			
			$\frac{ w_{\neq 0} }{ w }$ %	Pruning	Fast Prediction	Maximum Compression
LeNet-300-100	1.6	DC	8.0	6 (1.6)	-	40 (1.6)
		DNS	1.8	28* (2.0)	-	-
		SWS	4.3	12* (1.9)	-	64(1.9)
		Sparse VD	2.2	21(1.8)	84(1.8)	113 (1.8)
		GNJ	10.8	9(1.8)	36(1.8)	58(1.8)
		GHS	10.6	9(1.8)	23(1.9)	59(2.0)
LeNet-5-Caffe	0.9	DC	8.0	6*(0.7)	-	39(0.7)
		DNS	0.9	55*(0.9)	-	108(0.9)
		SWS	0.5	100*(1.0)	-	162(1.0)
		Sparse VD	0.7	63(1.0)	228(1.0)	365(1.0)
		GNJ	0.9	108(1.0)	361(1.0)	573(1.0)
		GHS	0.6	156(1.0)	419(1.0)	771(1.0)
VGG	8.4	GNJ	6.7	14(8.6)	56(8.8)	95(8.6)
		GHS	5.5	18(9.0)	59(9.0)	116(9.2)

← Compression rate of a factor 700x with no loss in accuracy!

# Part IV: Deep Art

# AI & Kunst









# De Visuele Turing Test



VS



van Gogh et  
al.

CN  
N



# De Visuele Turing Test



van Gogh et al.



CN  
N



John Singer Sargent  
"White Ships"



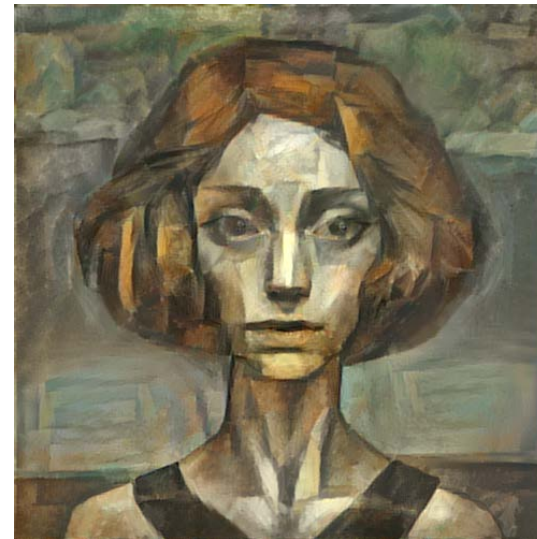
# De Visuele Turing Test



van Gogh et  
al.



CN  
N



# De Visuele Turing Test



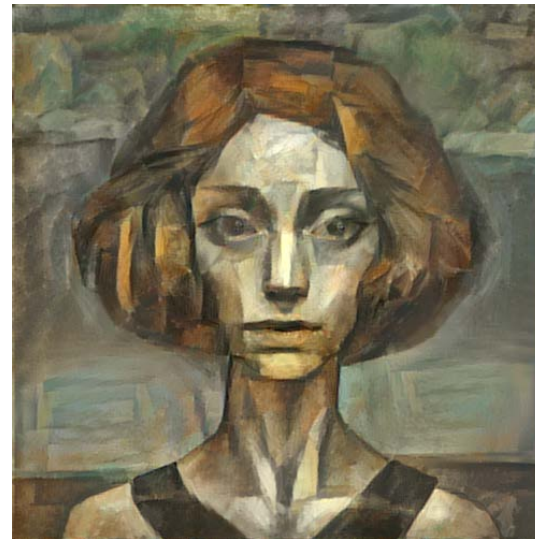
van Gogh et  
al.



CN  
N



Leroy Neiman  
"Mickey Mantle"



# Conclusions



Deep Learning is fun! (Deepdream)

- Deep Learning is a huge hammer that could be interesting to physics...
- Physics technology is now making inroads into deep learning (it's a good time to enter the field)
- We discussed:
  1. Lie groups and symmetry transformations to understand equivariance
  2. Variational free energies to for probabilistic / Bayesian deep learning

# Acknowledgements

